

Midterm Answers

- Survivor bias. They omitted funds that existed 5 years ago and are no longer around. When Vanguard included funds that existed 5 years ago and subsequently folded, the percent that beat the market fell to 46%. (This was actually a study of large cap funds.)
- The year 1987 is omitted and the data are not adjusted for the increase in the price level or in the number of households.
- They are equally likely to have a positive return because their Z-values are equal:

$$Z_1 = \frac{0-5}{10} = -0.5$$

$$Z_2 = \frac{0-10}{20} = -0.5$$

- The same as the probability of picking any six numbers:

$$\frac{6}{47} \frac{5}{46} \frac{4}{45} \frac{3}{44} \frac{2}{43} \frac{1}{42}$$

- The six coins are equally likely to be chosen. Of the 3 gold coins, 2 are in the double-gold drawer. So, the probability that you chose the double-gold drawer is 2/3. Therefore, sticking with the drawer you chose has a 2/3 probability of yielding a gold coin.

This can also be done via Bayes' Rule, letting  $GG$  be the double-gold drawer and letting  $PG$  be "pick a gold coin."

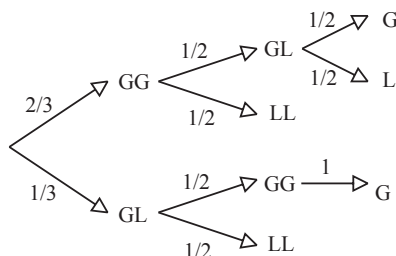
$$P[GG \text{ if } PG] = \frac{P[GG]P[PG \text{ if } GG]}{P[GG]P[PG \text{ if } GG] + P[GS]P[PG \text{ if } GS] + P[SS]P[PG \text{ if } SS]}$$

$$= \frac{(1/3)(1)}{(1/3)(1) + (1/3)(1/2) + (1/3)(0)}$$

$$= 2/3$$

[Not asked] If you switch, there is a 2/3 probability you initially chose the double-gold drawer, in which case you have an equal chance of choosing the double-lead or gold-lead drawer; if you do choose the lead-gold drawer, there is 1/2 probability of choosing the gold coin. There is a 1/3 probability that you initially chose the gold-lead drawer, in which case you have an equal chance of choosing the double-lead or double-gold drawer; if you do choose the double-gold drawer, you are certain to choose a gold coin.

Overall, if you switch, the probability of getting a gold coin is  $(2/3)(1/2)(1/2) + (1/3)(1/2)(1) = 1/3$



6. Outliers

7. a. The calculation assumes independence, but there may be genetic or environmental factors that contradict this assumption.  
b. This reverses the conditional probabilities.  $P[2 \text{ deaths if innocent}] \neq P[\text{innocent if 2 deaths}]$
8. a. Whatever team number Ocean gets, each of the other 15 students has an equal chance of being on Ocean's team:  $1/15$ .  
b. The probability that Ocean and Cove will be on the same team at least once in 12 weeks is equal to 1 minus the probability that they will never be on the same team:  $1 - (14/15)^{12} = 0.56$
9. The probability of making a shot is not constant because shots are taken from different locations and with differing amounts of defensive pressure.
10. Self-selection bias. Perhaps those most at risk of reconviction were more likely to be given talk therapy.